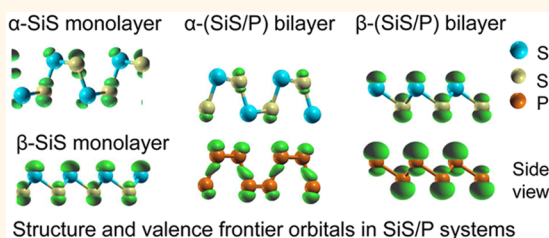


Designing Isoelectronic Counterparts to Layered Group V Semiconductors

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ABSTRACT In analogy to III–V compounds, which have significantly broadened the scope of group IV semiconductors, we propose a class of IV–VI compounds as isoelectronic counterparts to layered group V semiconductors. Using *ab initio* density functional theory, we study yet unrealized structural phases of silicon monosulfide (SiS). We find the black-phosphorus-like α -SiS to be almost equally stable as the blue-phosphorus-like β -SiS. Both α -SiS and β -SiS monolayers display a significant, indirect band gap that depends sensitively on the in-layer strain. Unlike 2D semiconductors of group V elements with the corresponding nonplanar structure, different SiS allotropes show a strong polarization either within or normal to the layers. We find that SiS may form both lateral and vertical heterostructures with phosphorene at a very small energy penalty, offering an unprecedented tunability in structural and electronic properties of SiS–P compounds.



KEYWORDS: silicon sulfide · isoelectronic · phosphorene · *ab initio* · electronic band structure

Two-dimensional semiconductors of group V elements, including phosphorene and arsenene, have been rapidly attracting interest due to their significant fundamental band gap, large density of states near the Fermi level, and high and anisotropic carrier mobility.^{1–4} Combination of these properties places these systems very favorably in the group of contenders for 2D electronics applications beyond graphene^{5,6} and transition metal dichalcogenides.⁷ Keeping in mind that the scope of group IV semiconductors such as Si has been broadened significantly by introducing isoelectronic III–V compounds, it is intriguing to see whether the same can be achieved in a new class of IV–VI compounds that are isoelectronic to group V elemental semiconductors. Even though this specific point of view has not yet received attention, there has been interest in specific IV–VI compounds, such as SnS, SnSe, and GeTe, for thermoelectric and photovoltaic applications.^{8–10} It appears likely that a specific search for isoelectronic counterparts of layered semiconductors such as phosphorene and arsenene may guide us to yet unexplored 2D semiconducting IV–VI compounds that are stable and flexible and display a tunable band gap.

As a yet unexplored IV–VI compound, we study the layered structure of silicon

monosulfide (SiS). We use *ab initio* density functional theory (DFT) to identify stable allotropes and determine their equilibrium geometry and electronic structure. We have identified two nearly equally stable allotropes, namely, the black-phosphorus-like α -SiS and the blue-phosphorus-like β -SiS, and show their structure in Figure 1a and d. Both α -SiS and β -SiS monolayers display a significant, indirect band gap that depends sensitively on the in-layer strain. Unlike 2D semiconductors of group V elements with the corresponding nonplanar structure, different SiS allotropes show a strong polarization either within or normal to the layers. We find that SiS may form both lateral and vertical heterostructures with phosphorene at a very small energy penalty, offering an unprecedented tunability in structural and electronic properties of SiS–P compounds.

RESULTS AND DISCUSSION

Since all atoms in sp^3 -layered structures of group V elements are 3-fold coordinated, the different allotropes can all be topologically mapped onto the honeycomb lattice of graphene with two sites per unit cell.¹¹ An easy way to generate IV–VI compounds that are isoelectronic to group V monolayers is to occupy one of these sites by a group IV and the other by a group VI element. In this way, we have generated

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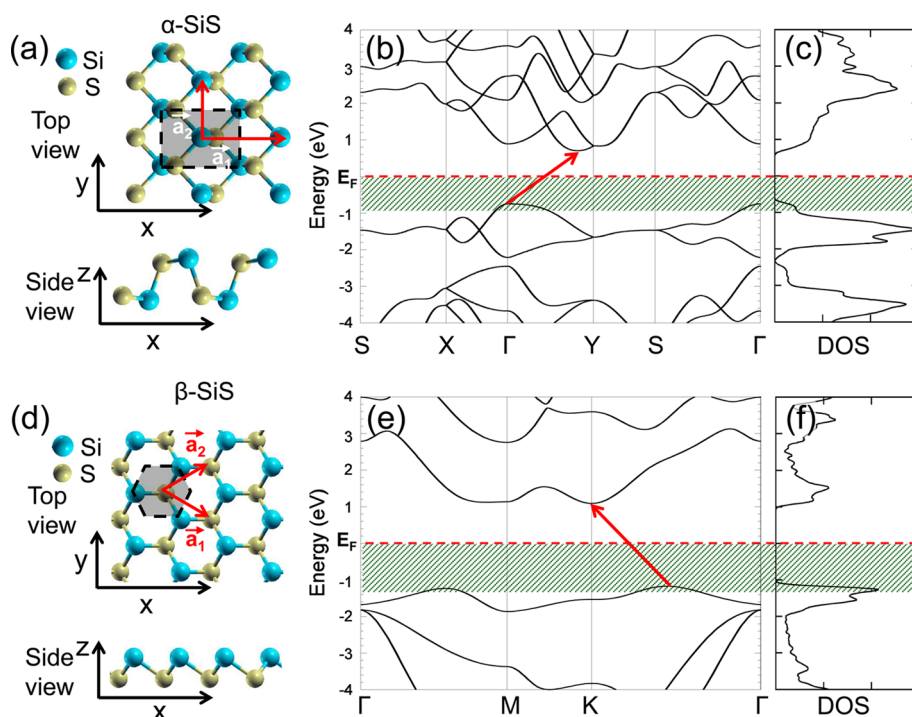


Figure 1. Atomic and electronic structure of (a–c) α -SiS and (d–f) β -SiS monolayers. (a and d) Ball-and-stick models of the geometry, with S and Si atoms distinguished by size and color and the Wigner–Seitz cell indicated by the shaded region. (b and e) Electronic band structure and (c and f) the electronic density of states (DOS) of the systems. The energy range between E_F and 0.2 eV below the top of the valence band, indicated by the green shading, is used to identify valence frontier states.

the orthorhombic α -SiS monolayer structure, shown in Figure 1a, from a monolayer of black phosphorene (or α -P). The hexagonal β -SiS monolayer, shown in Figure 1d, has been generated in the same way from the blue phosphorene (or β -P) structure.

The monolayer structures have been optimized using DFT with the Perdew–Burke–Ernzerhof (PBE)¹² exchange–correlation functional, as discussed in the Methods section. We found that the presence of two elements with different local bonding preferences increases the thickness of the SiS monolayers when compared to the phosphorene counterparts. The 2D lattice of α -SiS is spanned by the orthogonal Bravais lattice vectors $|\vec{a}_1| = 4.76 \text{ \AA}$ and $|\vec{a}_2| = 3.40 \text{ \AA}$, which are about 3% longer than the lattice vectors of black phosphorene. The 2D hexagonal lattice of β -SiS is spanned by two Bravais lattice vectors $a = |\vec{a}_1| = |\vec{a}_2| = 3.35 \text{ \AA}$, which are $\approx 1\%$ longer than those of blue phosphorene. Unlike in the counterpart structures of the phosphorene monolayer, we find β -SiS to be more stable by about 12 meV/atom than α -SiS. We checked the phonon spectrum of free-standing α -SiS and β -SiS monolayers and found no soft modes that would cause a spontaneous collapse of the structure.

An apparently different layered SiS structure had been synthesized¹³ by exposing the layered CaSi_2 structure to S_2Cl_2 . It appears that the S_2Cl_2 reagent reacted with the Ca atoms intercalated between silicene layers in CaSi_2 by forming CaCl_2 and saturating

the valencies of the silicene layers by $-\text{S}-\text{S}$ bridges. Even though no structural information has been provided in that study, we identified a likely candidate structure and found it to be less stable than the postulated SiS allotropes, on which we focus next.

Since the electronegativity of S is higher than that of Si, we expect an electron transfer from Si to S atoms. On the basis of a Mulliken population analysis, we estimate a net transfer of 0.3 electron in α -SiS and 0.2 electron in β -SiS from silicon to sulfur atoms. This charge redistribution, combined with the nonplanarity of the structure, causes a net polarization. We find an in-plane polarization for α -SiS and an out-of-plane polarization for β -SiS.

Whereas DFT generally provides an accurate description of the total charge density and equilibrium geometry, interpretation of Kohn–Sham energy eigenvalues as quasiparticle energies is more problematic. Still, we present our DFT-PBE results for the electronic structure of α -SiS and β -SiS monolayers in Figure 1. Even though the fundamental band gaps are typically underestimated in this approach, the prediction that both systems are indirect-gap semiconductors is likely correct. Our calculated band structure and the corresponding density of states for α -SiS, presented in Figure 1b,c, suggest that the fundamental band gap value $E_g = 1.44 \text{ eV}$ should be significantly larger than in the isoelectronic black phosphorene counterpart. The band structure near the top of the

valence band shows a significant anisotropy when comparing the Γ - X and Γ - Y directions. In analogy to phosphorene, α -SiS should exhibit a higher hole mobility along the x -direction than along the y -direction.

The DFT-based fundamental band gap $E_g = 2.26$ eV in the monolayer of β -SiS is even larger. The band structure in the symmetric honeycomb lattice of β -SiS is rather isotropic, as seen in Figure 1e. The top of the valence band is very flat, resulting in a heavy hole mass and a large density of states (DOS) in that region, as seen in Figure 1f.

The character of frontier states not only is of interest for a microscopic understanding of the conduction channels but is also crucial for the design of optimum contacts.¹⁴ Whereas DFT-based band gaps are typically underestimated as mentioned above, the electronic structure of the valence and the conduction band region in DFT is believed to closely correspond to experimental results. In Figure 2, we show the charge density associated with frontier states near the top of the valence band. These states, which correspond to the energy range highlighted by the green shading in the band structure of α -SiS in Figure 1b and that of β -SiS in Figure 1e, cover the energy range between the

midgap and 0.2 eV below the top of the valence band. The valence frontier states of α -SiS in Figure 2a and β -SiS in Figure 2b are similar in spite of the notable charge density differences caused by the larger DOS of β -SiS in this energy range. The difference between S and Si atoms is also reflected in the character of the valence frontier states at these sites. Whereas p_z states contribute most at sulfur sites, silicon sites contribute a mixture of s and p_z states. These frontier states differ from those of phosphorene, which are related to lone pair electron states.

Similar to phosphorene, the fundamental band gap value of SiS also depends sensitively on the in-layer strain, as seen in Figure 3. Due to their nonplanarity, accordion-like in-layer stretching or compression of SiS structures may be achieved at little energy cost, as shown in the Supporting Information. The energy cost is particularly low for a deformation along the soft x -direction, requiring $\lesssim 20$ meV/atom to induce a $\pm 9\%$ in-layer strain. We believe that in view of the softness of the structure similar strain values may be achieved during epitaxial growth on particular incommensurate substrates. We also note that tensile strain values such as these have been achieved experimentally in suspended graphene membranes that are much more resilient to stretching due to their planar geometry and stronger bonds.¹⁵⁻¹⁷ Consequently, we believe that strain engineering is a viable way to effectively tune the fundamental band gap in these systems.

Our results for α -SiS in Figure 3a indicate that the band gap decreases when the structure is compressed and increases slightly when it is stretched. The largest change in the band gap, namely, its reduction to 0.3 eV, may be achieved during a 9% compression. As seen in Figure 3b, we expect the fundamental band gap of β -SiS to be reduced during both stretching and compression. Within the $\pm 9\%$ range, we find that the band gap may be tuned in the range from ~ 1.0 to 2.3 eV. This high degree of band gap tunability in SiS appears particularly attractive for potential applications in flexible electronics.

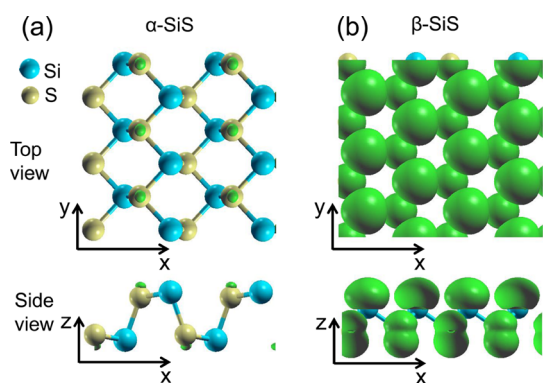


Figure 2. Electron density ρ_{vb} associated with states in the energy range between the Fermi level E_F and 0.2 eV below the top of the valence band, shown by the shaded region in Figure 1, in a monolayer of (a) α -SiS and (b) β -SiS. $\rho_{vb} = 2.5 \times 10^{-3}$ e/ \AA^3 contours are superposed with ball-and-stick models of related structures.

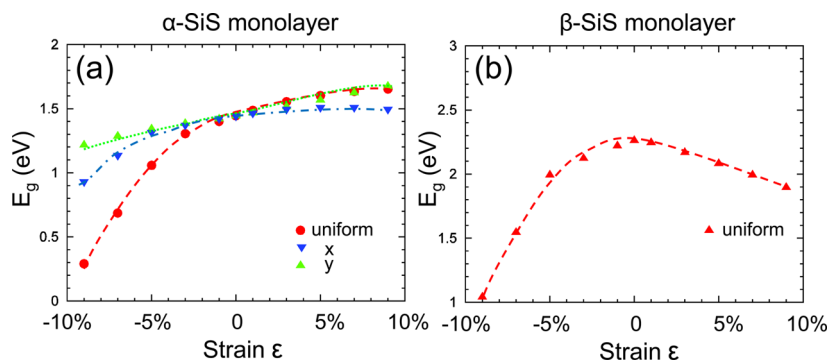


Figure 3. Electronic band gap of (a) α -SiS and (b) β -SiS monolayers as a function of the in-layer strain. Besides the uniform strain, we also show results for uniaxial strain along the x - and y -direction in the anisotropic structure of α -SiS in (a). The lines are guides to the eye.

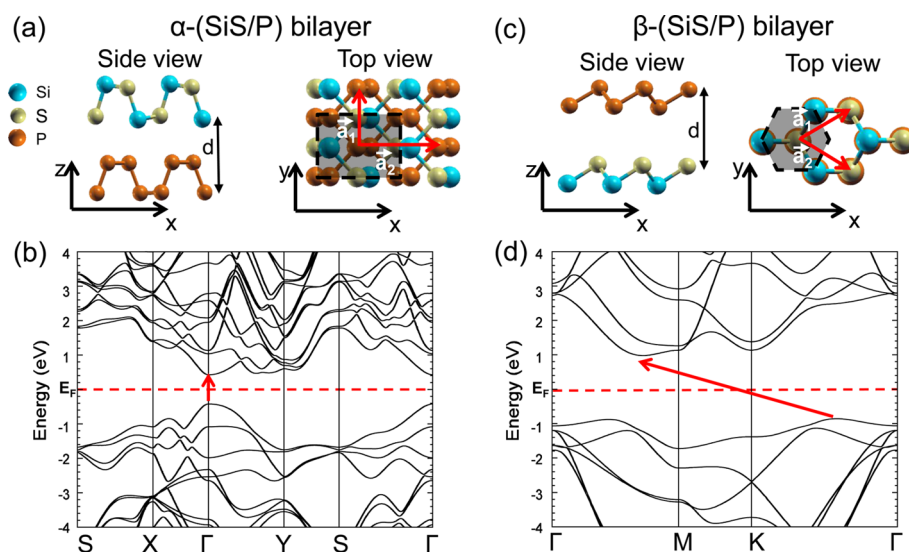


Figure 4. Optimum geometry and electronic band structure of (a and b) an α -(SiS/P) bilayer and (c and d) a β -(SiS/P) bilayer. The optimum stacking of the SiS and the phosphorene monolayers in the α -(SiS/P) bilayer in (a) is AB and that in the β -(SiS/P) bilayer is AA.

Since the geometry and lattice constants of SiS and phosphorene are very similar, it is likely that the two could interface naturally in lateral and vertical heterostructures, thus further advancing the tunability of their electronic properties. In Figure 4, we present electronic structure results for bilayers consisting of a SiS and a phosphorene monolayer in both α - and β -phases as the simplest examples of vertical heterostructures. We have optimized the bilayer structures assuming commensurability, *i.e.*, setting the primitive unit cells of each monolayer to be the same. The optimum geometry of the α -(SiS/P) bilayer is shown in Figure 4a, and that of the β -(SiS/P) bilayer in Figure 4c.

We find the interlayer interaction in the two bilayer systems to be rather weak, amounting to ≈ 20 meV/atom based on our DFT-PBE calculations. Taking better account of van der Waals interactions would likely increase the calculated interaction energy and reduce the large interlayer separation of $d \approx 5.4$ Å. Whereas the precise interlayer interaction and separation are not of primary concern here, our most important finding is that the weak interaction is not purely dispersive in nature, since we find a substantial rehybridization of states between the adjacent SiS and phosphorene layers. Consequently, as we show more explicitly in the Supporting Information, the bilayer band structure is not a mere superposition of the two monolayer band structures in the same assumed geometry.

As shown in Figure 4b, the α -(SiS/P) bilayer is a direct-gap semiconductor with $E_g \approx 0.8$ eV, smaller than the band gap in either isolated monolayer. Since the gap is indirect in the α -SiS monolayer, whereas it is direct in α -P, the cause for the direct band gap in α -SiS/P may be the dominance of P states near the gap.

We find this conjecture confirmed by examining the frontier orbitals of the bilayer. As we show in the Supporting Information, the frontier states in the conduction band region of the bilayer are essentially purely P-based, whereas those in the valence band region have only a small contribution from the SiS layer.

The electronic band structure of the AA-stacked β -(SiS/P) bilayer is presented in Figure 4d. The fundamental band gap is indirect in this system, and its value $E_g \approx 1.7$ eV is again smaller than in isolated blue phosphorene and β -SiS monolayers. As seen in the Supporting Information, also the frontier states of β -(SiS/P) are dominated by P orbitals both in the valence and the conduction band region.

Since both SiS and phosphorene are rather flexible, they may adjust to each other and form also in-layer heterostructures at little or no energy penalty. We constructed two types of SiSP₂ heterostructures for both α and β allotropes and show their geometry and electronic structure in Figure 5. One type of heterostructure, shown in Figure 5a and e, contains P–P and Si–S atom pairs completely separated from like atom pairs. The other type of heterostructure, presented in Figure 5c and g, contains alternating, contiguous SiS and phosphorus chains. These structures maintain a rectangular lattice with four atoms per unit cell. Generally, we found the in-layer heterostructures to be less stable than pure phosphorene and SiS monolayers. The least stable heterostructures among these are those with isolated P–P or Si–S atom pairs, shown in Figure 5a and e, which are ~ 0.2 eV/atom less stable than SiS and phosphorene monolayers due to their highly frustrated geometries. The heterostructures with contiguous phosphorus and SiS chains, presented in Figure 5c and g, may better optimize the nearest-neighbor environment. This causes less frustration,

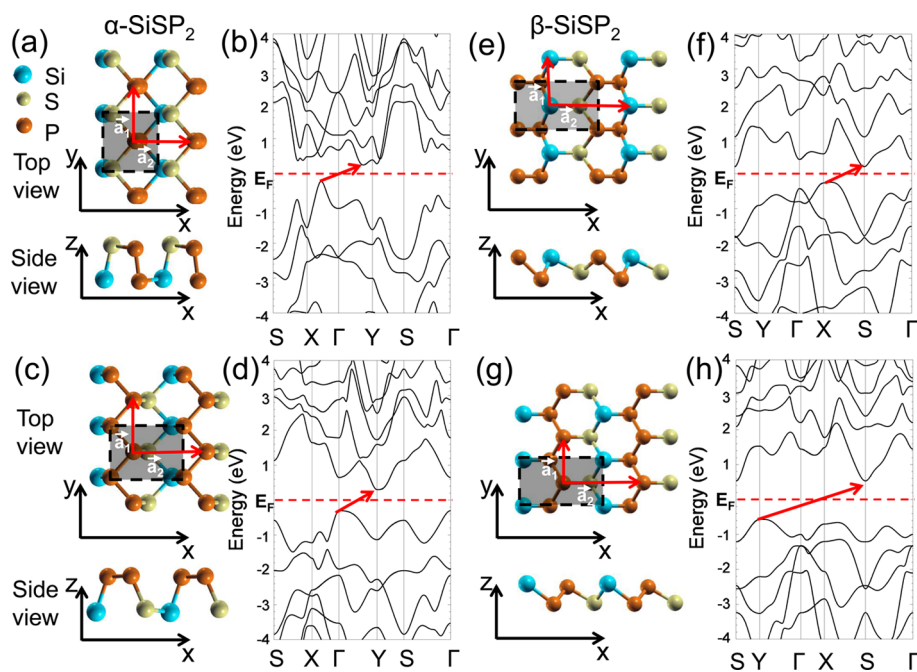


Figure 5. Optimum geometry and electronic band structure of (a–d) two different in-layer heterostructures of α -SiSP₂ and (e–h) two different in-layer heterostructures of β -SiSP₂. The heterostructures differ in the arrangement of P atoms.

making these systems only ~ 0.1 eV/atom less stable than isolated SiS and phosphorene monolayers.

We found all four in-layer heterostructures to be indirect-gap semiconductors. As in the vertical heterostructures, we found the fundamental band gaps to be substantially smaller than in isolated SiS and phosphorene monolayers. As seen in Figure 5a,b and 5e,f, the fundamental band gap E_g is close to 0.5 eV in the less stable heterostructures with isolated Si–S and P–P pairs. We found larger band gap values in the more stable heterostructures with contiguous SiS and P chains, namely, $E_g \approx 0.6$ eV in α -SiSP₂ shown in Figure 5c,d and $E_g \approx 1.1$ eV in β -SiSP₂ shown in Figure 5g,h, both nearly half the value of the smaller band gap in either SiS or phosphorene monolayers. These findings indicate an intriguing possibility of isoelectronic doping as an effective way to tune the electronic properties of SiSP_n systems.

In view of the different successful synthesis approaches used to form layered IV–VI compounds such as SiS¹³ or SnS¹⁸ with a structure similar to α -SiS, we believe that a suitable synthesis path will be found to form also the allotropes introduced in this study. The weak interlayer interaction in layered pure SiS compounds or SiS/P heterostructures should allow for a mechanical exfoliation yielding monolayers and bilayers, the same as in graphene and phosphorene. Chemical vapor deposition (CVD), which had been used successfully in the past to grow graphene^{19,20} and silicene,²¹ may become ultimately the most common approach to grow few-layer SiS on specific substrates.

As suggested above, compounds that are isoelectronic to group V layered semiconductors are not

limited to pure IV–VI systems, but may contain other group V elements in the same layer or in a vertical few-layer heterostructure. The initial interest in black phosphorene could thus be significantly expanded by considering the whole range of group IV elements including Si, Ge, Sn, and Pb, group VI elements such as S, Se, and Te, and group V elements such as P, As, Sb, and Bi, leading to a virtually limitless number of compounds and structural phases. The large family of IV–VI systems that are isoelectronic to group V elemental semiconductors will include 2D semiconductors with a sizable fundamental band gap, a high carrier mobility, and chemical stability. Expanding this family to heterostructures containing also group V elements should provide a way to effectively tune the electronic properties of the pristine structures, which will likely bring unlimited richness to the field of 2D semiconductors.

CONCLUSIONS

In conclusion, we have proposed IV–VI compounds as isoelectronic counterparts to layered group V semiconductors in analogy to III–V compounds, which have significantly broadened the scope of group IV semiconductors. Using *ab initio* density functional theory, we have identified yet unrealized structural phases of silicon monosulfide including the black-phosphorus-like α -SiS and the almost equally stable blue-phosphorus-like β -SiS. We found that both α -SiS and β -SiS monolayers display a significant, indirect band gap that depends sensitively on the in-layer strain. Unlike 2D semiconductors of group V elements with the corresponding nonplanar structure, different SiS allotropes are polar. We found that SiS may form

both lateral and vertical heterostructures with phosphorene at a very small energy penalty, offering an unprecedented tunability in structural and electronic properties of SiS-P compounds. Combining other

group IV and group VI elements with group V elements is expected to lead to a large family of layered semiconductors with an unprecedented richness in structural and electronic properties.

METHODS

Our computational approach to study the equilibrium structure, stability, and electronic properties of SiS structures is based on *ab initio* density functional theory with the Perdew–Burke–Ernzerhof¹² exchange–correlation functional as implemented in the SIESTA²² and VASP^{23–26} codes. We use periodic boundary conditions throughout the study, with few-layer structures represented by a periodic array of slabs separated by a vacuum region of ≥ 15 Å. In our SIESTA calculations we used norm-conserving Troullier–Martins pseudopotentials²⁷ and a double- ζ basis including polarization orbitals. The reciprocal space has been sampled by a fine grid²⁸ of $8 \times 8 \times 1$ k-points in the Brillouin zone of the primitive unit cell of the 2D structures. We used a mesh cutoff energy of 180 Ry to determine the self-consistent charge density, which provided us with a precision in total energy of ≤ 2 meV/atom. In VASP calculations, we used an energy cutoff of 500 eV and the same k-point sampling as mentioned above. All geometries have been optimized using the conjugate gradient method,²⁹ until none of the residual Hellmann–Feynman forces exceeded 10^{-2} eV/Å. Equilibrium structures and energies based on SIESTA have been checked against values based on the VASP code.

Conflict of Interest: The authors declare no competing financial interest.

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Supporting Information Available: Energy–strain relationship in SiS and character of frontier states in SiS/P bilayers in the α and β phases, as well as vibrational spectra of α - and β -SiS monolayers. The Supporting Information is available free of charge on the ACS Publications website at DOI: 10.1021/acs.nano.5b02742.

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